

# Overview

Goal: provide a practical and interpretable tool for analyzing 3D scenes for aerial surveying and mapping, without relying on application-specific user annotations.

Approach: a probabilistic reconstruction model that decomposes inputs into a set of learned prototypical 3D shapes, for unsupervised instance/semantic segmentation.



### Learnable shape prototypes:

Following [4], we define K point clouds  $\mathbf{P}^1, \dots, \mathbf{P}^K$  that we refer to as *prototypes*. Each prototype is meant to represent a single instance of a recurring 3D structure in the considered scene  $\mathbf{X}$ . The points' coordinates are free parameters of the model.

### Scene reconstruction model:

$$\mathcal{M}(\mathbf{X}) = \bigcup_{\substack{s=1\cdots S\\a_s=1}} \mathcal{M}_s(\mathbf{X}) \text{, with } \mathcal{M}_s(\mathbf{X}) = \mathbf{Y}_s^k = \mathcal{T}_s(\mathbf{X})[\mathbf{P}^k] \text{ if } b_s = k \text{.}$$

### Probabilistic modeling:

a and b as random variables following (multi)-Bernoulli distributions;  $p(a_s = 1) = \alpha_s$ : probability that the slot s is activated;

 $p(a_s = 1, b_s = k) = \beta_s^k$ : probability it is activated and selects prototype k.

### **Unsupervised training losses:**

Slots average of the expected distance between  $\mathcal{M}_s(\mathbf{X})$  and  $\mathbf{X}$ :

Average over all points x of X of the expected distance between x and its closest point in the reconstruction:

 $\mathcal{L}_{\mathsf{acc}}(\mathcal{M}, \mathbf{X}) = \frac{1}{S} \sum_{s=1}^{S} \mathbb{E}_{a_s, b_s} \left[ d\left( \mathcal{M}_s(\mathbf{X}), \mathbf{X} \right) \right] \,.$ 

$$\mathcal{L}_{\text{cov}}(\mathcal{M}, \mathbf{X}) = \frac{1}{|\mathbf{X}|} \sum_{x \in \mathbf{X}} \mathbb{E}_{a, b} \left[ \min_{s \mid a_s = 1} d(x, \mathcal{M}_s(\mathbf{X})) \right].$$

The final unsupervised loss is the sum of reconstruction losses and regularization:

 $\mathbb{E}_{\mathbf{X}}\left[\mathcal{L}_{\mathsf{acc}}\left(\mathcal{M}, \mathbf{X}\right) + \mathcal{L}_{\mathsf{cov}}\left(\mathcal{M}, \mathbf{X}\right)\right] + \lambda_{\mathsf{act}}\mathcal{L}_{\mathsf{act}} + \lambda_{\mathsf{slot}}\mathcal{L}_{\mathsf{slot}} + \lambda_{\mathsf{proto}}\mathcal{L}_{\mathsf{proto}}.$ 

Bibliography: [1] Paschalidou *et al.* Superquadrics revisited: Learning 3d shape parsing beyond cuboids. CVPR19. [2] Monnier *et al.* Unsupervised layered image decomposition into object prototypes. ICCV21. [3] Deprelle *et al.* Learning elementary structures for 3D shape generation and matching. NeurIPS19. [4] Loiseau *et al.* Representing Shape Collections with Alignment-Aware Linear Models. 3DV21. [5] IGN (French mapping agency). LiDAR-HD: A 3D mapping of France's soil and subsoil, 2021. Acknowledgements: This work was supported by ANR project READY3D ANR-19-CE23-0007, ANR under the France 2030 program (ANR-23-PEIA-0008), and HPC resources of IDRIS made by GENCI. The work of MA was partly and subsoil, 2021. Acknowledgements: This work was supported by ANR project READY3D ANR-19-CE23-0007, ANR under the France 2030 program (ANR-23-PEIA-0008), and HPC resources of IDRIS made by GENCI. The work of MA was partly and subsoil, 2021. Acknowledgements: This work was supported by ANR project READY3D ANR-19-CE23-0007, ANR under the France 2030 program (ANR-23-PEIA-0008), and HPC resources of IDRIS made by GENCI. The work of MA was partly and subsoil and subs supported by the European Research Council (ERC project DISCOVER, number 101076028). The scenes of Earth Parser Dataset were acquired and feedback. E. Blettery, N. Dufour, A. Guedon, H. Mair Rawsthorne, T. Monnier, D. Robert, M. Petrovich and Y. Siglidis for inspiring discussions and feedback.

# Learnable Earth Parser: Discovering 3D Prototypes in Aerial Scans

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# Earth Parser Dataset



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### Learnable Earth Parser

Earth Parser Dataset: Annotated aerial LiDAR scans in diverse real-world environments.

# Unsupervised Qualitative and Quantitative Results







### Method Overview.

• Our model approximates an input point cloud  $\mathbf{X}$  with S slot models.

• Each slot maps X to an affine 3D deformation  $\mathcal{T}_s(\mathbf{X})$ , a slot activation probability  $\alpha_s$ , and the joint probabilities  $\beta_s^1, \dots, \beta_s^K$  of the slot being activated and choosing one of the K prototype point clouds  $\mathbf{P}^1, \dots, \mathbf{P}^K$ .

• The output  $\mathcal{M}_s(\mathbf{X})$  of an activated slot s is obtained by applying  $\mathcal{T}_s(\mathbf{X})$ to its most likely prototype.

 Non-activated slots do not contribute to the output.

Image: selection of the selec	tediction		Input		Pred	iction	
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Crop fields	Forest	Greenhouses	Marina	Power pla	nt Urba	an N	Nindturbin

Crop fields Cham. mloU		Forest Cham. mloU		Greenhouses Cham. mIoU		Marina Cham. mloU		Power plant Cham. mloU		Urban Cham. mIoU		Windturbines Cham. mIoU	
0.86		1.04		0.60		0.93	—	0.58		0.40		13.50	
6.10	83.2	14.59	40.2	5.36	42.0	6.16	41.4	5.36	29.0	2.99	47.3	36.19	25.9
1.07	43.1	1.58	71.4	0.56	49.1	0.73	42.1	0.45	41.6	0.63	48.8	9.47	48.1
0.72	96.9	0.88	83.7	0.40	91.3	0.82	78.7	0.44	52.2	0.29	83.2	6.65	93.4

